Labor Market Competition and Inequality

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Labor market inequality

- Traditional (competitive) view of wage inequality \rightarrow you earn what you are
 - supply side, e.g., schooling
 - demand side, e.g., biased technological change
 - institutions, e.g., minimum wage

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 - wage differences across firms, regardless of the "who" (Card, Cardoso, Heining, and Kline, 2018)
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 - employer market power is a global phenomenon (Manning, 2021, Armangué-Jubert, Guner, and Ruggieri, 2024)
- Monopsony theory: labor market power gives firms the power to set wages → higher degree of wage inequality (Robinson, 1933; Burdett and Mortensen, 1998; Manning, 2003)

This paper in a nutshell

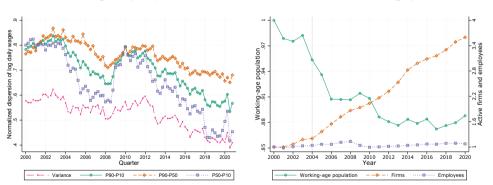
- Does wage inequality and labor market competition evolve together?
 - cross-sectional evidence suggests higher inequality in less competitive markets (e.g., Weber, 2015; Bassier, 2023)
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- Does wage inequality and labor market competition evolve together?
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 - what about the dynamics? This paper
- Using Lithuanian Social Security data spanning two decades
 - 1. the role of firm-specific wage components in wage inequality over development
 - firms explain almost entirely the dynamics of inequality along the development path
 - 2. the evolution of labor market competition over economic growth
 - negative gradient between firm's labor market power and economic growth
 - 3. do they move together?
 - simple accounting exercise suggests could contribute to about 17%
 - 4. our suspect: EU accession
 - not today... work in progress

Why Lithuania?

Wage inequality

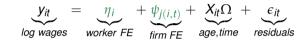


Labor market demographics

more stylized facts

Firms and workers in the variance of wages

From the AKM model (Abowd, Kramarz, and Margolis, 1999)



to the variance decomposition

$$var(y_{it}) = var(\eta_i) + var(\psi_{j(i,t)}) + var(X_{it}\Omega) + var(\epsilon_{it}) + 2 \times \left[\underbrace{cov(\eta_i, \psi_{j(i,t)})}_{sorting} + cov(\eta_i, X_{it}\Omega) + cov(\psi_{j(i,t)}, X_{it}\Omega)\right]$$

identifying assumptions

Social Security data

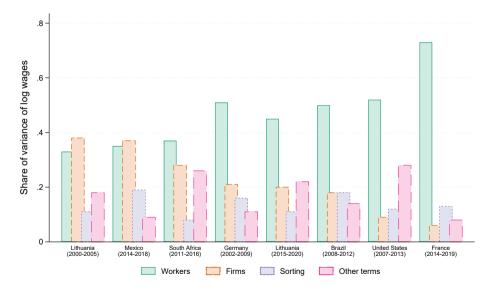
- Administrative data from the State Social Insurance Fund Board (SoDra)
 - 25% random sample of the Social Security population in 2000-2020
 - workers: identifier, gender, age, employment status, length of the employment relationship, insured labor income but no hours or education info!
 - firms: identifier, location, sector, wage bill, and firm size at the end of the year

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 - workers: identifier, gender, age, employment status, length of the employment relationship, insured labor income but no hours or education info!
 - firms: identifier, location, sector, wage bill, and firm size at the end of the year
- Estimation sample
 - quarterly panel of private sector workers, 2000Q1 to 2020Q4
 - main job workers employed for ${\geq}15 \text{days}$ & earning ${\geq}0.5{\times}\text{monthly}$ MW in a quarter
 - wage metric: real daily wages = quarterly labor earnings / days worked in the quarter
 - cleaned data: 532,500 workers in 143,177 firms over 16,735,075 observations
 - connected set: 526,549 workers in 137,514 firms over 16,637,948 observations

summary statistics

Contribution of firms and workers to inequality resembles development



time-varying effects

estimation sample le

leave-one-out estimator

firm clusters

Compression of firm-specific wage components key factor behind the fall in inequality

| | 2000 | -05 to 20 | 15-20 |
|---|--------|-----------|--------|
| | AKM | KSS | BLM |
| Change in $Var(y)$ | -0.131 | -0.136 | -0.123 |
| Contribution | | | |
| $Var(\eta)$ | -0.088 | -0.043 | -0.233 |
| $Var(\psi)$ | 0.898 | 0.930 | 0.639 |
| $Var(X\Omega)$ | -0.067 | -0.068 | -0.148 |
| $Var(\epsilon)$ | 0.058 | 0.059 | 0.096 |
| $2 \times Cov(\eta, \psi)$ | 0.184 | 0.109 | 0.504 |
| $2 \times Cov(\eta, X\Omega)$ | 0.036 | 0.038 | 0.121 |
| $2 \times Cov(\psi, X\Omega)$ | -0.021 | -0.024 | 0.022 |
| Counterfactual change in $Var(y)$ | | | |
| 1. Fixed variance of firm effects | -0.013 | -0.017 | -0.045 |
| 2. Fixed corr. of firm and worker effects | -0.117 | -0.150 | -0.109 |
| 3. Both 1 and 2 | 0.012 | -0.024 | 0.024 |

What can be behind this decline?

- Structural transformation: reallocation of labor towards sectors with lower dispersion of pay policies
 - FHK decomposition suggests is a within-sector phenomenon
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 - no clear correlation between more affected sectors and larger declines in firm-drive inequality MW

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- Policy: truncated pay distribution due to cumulative increase of the minimum wage ${\sim}x3$ in nominal terms
 - no clear correlation between more affected sectors and larger declines in firm-drive inequality MW
- Labor market competition?
 - monopsony theory: employer market power and firm-driven inequality are closely linked

Monopsony power and firm-driven wage inequality

- Dynamic monopsony model a la Manning (2003, 2021)
 - firms are heterogeneous in their productivity, *z_{jt}*
 - production function w/ decreasing returns to (homogeneous) labor, L_{jt}
 - firms face an upward-sloping labor supply curve labor that depends on recruitment, R(wjt), and separation, s(wjt) rates
- Optimal labor demand condition can be rearranged to show that

$$var[\log w_{jt}] \approx \left(\frac{1}{1+\varepsilon_t}\right)^2 var[\log z_{jt}]$$
 with $\varepsilon_t = \varepsilon_{Rt} - \varepsilon_{sept}$

- ε is elasticity of labor supply to wages of firm j
 - competitive model: $\varepsilon = \infty \Rightarrow$ the law of one price
 - imperfect competition: $\varepsilon < \infty \Rightarrow$ firm-specific wages result in firm-driven wage inequality
 - higher competition \implies lower firm-driven inequality
- Does labor market competition increased?

Estimating the firm labor supply elasticity \equiv labor market competition

$$P(s_{ijt} = 1) = \alpha + \beta \log w_{ijt} + X_{ijt}\Lambda + \xi_{ijt}$$

- s_{ijt} stands for the separation of worker *i* from employer *j* at quarter *t*
 - all separations and EE transitions at a quarterly frequency
- w_{ijt} is the corresponding wage measure
 - worker's wage or firm-specific wage component
- X_{iit} is a vector of controls
 - estimated AKM worker fixed effect + age, gender, industry, and time effects
- ξ_{ijt} is the error term

• Firm labor supply elasticity
$$\equiv -2 \times \frac{\hat{\beta}}{s_{ijt}}$$
 (Manning, 2003)

The firm's labor supply elasticity has increased over the last two decades

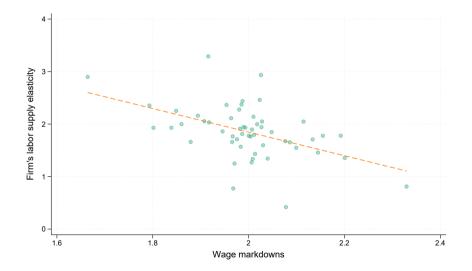
| A. 2000-2005 | 005 Worker wage | | Firm fixe | ed effect | IV-Firm fixed effect | | | |
|-------------------------|-----------------|-----------|-------------------|-----------|----------------------|----------------------|--|--|
| | Sep | EE Sep | Sep | EE Sep | Sep | EE Sep | | |
| | (1) | (2) | (3) | (4) | (5) | (6) | | |
| β | -0.0601 | -0.0250 | -0.0485 | -0.0220 | -0.0800 | -0.0433 | | |
| | (0.0004) | (0.0003) | (0.0019) | (0.0010) | (0.0024) | (0.0014) | | |
| ε _{LS} | 1.0329 | 0.9747 | 0.8327 | 0.8561 | 1.3746 | 1.6861 | | |
| | (0.0068) | (0.0104) | (0.0083) | (0.0125) | (0.0417) | (0.0556) | | |
| First stage F-statistic | | | | | -, | 2.27 | | |
| Observations | 4,149,923 | 4,149,923 | 4,149,923 | 4,149,923 | 4,149,923 | 4,149,923 | | |
| | | | | | | | | |
| B. 2015-2020 | Worker wage | | Firm fixed effect | | IV-Firm fi | IV-Firm fixed effect | | |
| | Sep | EE Sep | Sep | EE Sep | Sep | EE Sep | | |
| | (1) | (2) | (3) | (4) | (5) | (6) | | |
| β | -0.0773 | -0.0289 | -0.0565 | -0.0246 | -0.0979 | -0.0507 | | |
| , | (0.0005) | (0.0003) | (0.0015) | (0.0009) | (0.0023) | (0.0013) | | |
| ε _{LS} | 1.3693 | 1.1145 | 1.0007 | 0.9478 | 1.7340 | 1.9514 | | |
| 20 | (0.0216) | (0.0220) | (0.0265) | (0.0125) | (0.0415) | (0.0519) | | |
| First stage F-statistic | | | | | 13,757.87 | | | |
| Observations | 4,404,064 | 4,404,064 | 4,404,064 | 4,404,064 | 4,404,064 | 4,404,064 | | |

complementary log-log alternative set of controls

FLSE increasing likely to reflect competition rather than LM segmentation or concentration

- Worker heterogeneity can lead to market segmentation, affecting FLSE without real changes in competition
 - FLSE increased for both workers below and above the median of AKM worker FEs skill-specific flse
- With strategic interaction between employers as in Berger et al., 2022, FLSE can increase due to MW-induced changes in concentration
 - no correlation between ↑ FLSE and ∆wage bill-HHI or MW incidence firm granularity MW incidence

Elasticities resemble markdowns from producers data \rightarrow competition increased



Did labor market competition and firm-drive inequality move together?

 $\Delta \mathsf{var}_{st}[\psi_j] = \alpha + \beta \Delta \varepsilon_{st} + X_{st} \Omega + v_{st}$

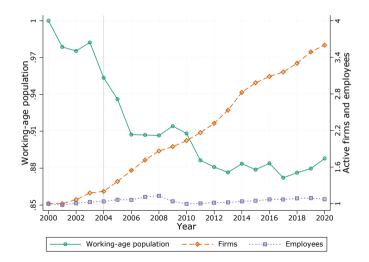
- $\Delta var_{st}[\psi_i]$ sector-specific changes in the variance of firm FE, 2000-05 to 2015-20
- $\Delta \varepsilon_{st}$ sector-specific changes in firm's labor supply elasticity, 2000-05 to 2015-20
- X sector-specific vector of controls
 - "model-based" \equiv firm's labor supply elasticity in 2015-20 + changes in firm's size dispersion
 - minimum wage workers in 2000-05, account for sustained MW hikes and potential reallocation effects (Dustmann et al., 2021)
 - changes in LM concentration, account for market structure dynamics and its impact on wage inequality (Deb et al., 2024)

Dispersion of firm pay policies negatively correlated with LM competition

| $\Delta \operatorname{Var}(\psi_i)$ | | | | | | | | |
|-------------------------------------|--------------|--------------|--------------|--------------|--------------|--------------|--|--|
| | A | ll seperatio | ns | | Job-to-job | | | |
| | OLS | OLS | ORIV | OLS | OLS | ORIV | | |
| | (1) | (2) | (3) | (4) | (5) | (6) | | |
| Δ Firm LSE | -0.0128 | -0.0137 | -0.0379 | -0.0126 | -0.0146 | -0.0422 | | |
| | (0.0047) | (0.0059) | (0.0180) | (0.0042) | (0.0043) | (0.0227) | | |
| Implied % Δ in inequality | 5.7 | 6.1 | 16.9 | 6.2 | 7.1 | 20.6 | | |
| Model-based controls | \checkmark | | | \checkmark | | | | |
| Full set of controls | | \checkmark | \checkmark | | \checkmark | \checkmark | | |
| No. sectors | 74 | 74 | 74 | 74 | 74 | 74 | | |

counterfactual calculation no correlation w/ WFE or sorting correlation stronger P50-P10 of FFE

Tightening labor market (LS \downarrow & LD \uparrow) after EU accession potential trigger for increased competition [*in progress*]



Taking stock

- Three main findings
 - firms play a critical role in declining inequality over Lithuania's development
 - labor market competition increased with economic growth
 - implied change in inequality due to the co-movement with competition = 17-20%
- Wage inequality can be consequence of market failures → labor market and competition policies can help tackle inequality and increase welfare
- Next step: link EU accession (outside options) and increases in competition



APPENDIX

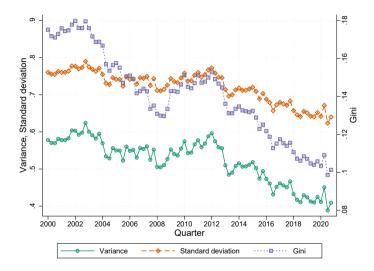
Lithuanian context to test whether labor market competition affects inequality

- The economy more than doubled in size ightarrow from low- to high-income country growth
- Sharp decline in wage inequality, e.g., Gini halved between 2000 and 2020 Gini and co.
 - MW flagship policy to boost income at the bottom, increased by ${\sim}235\%$ in real terms
- Critical changes in the labor market since joining the EU in 2004
 - (labor) market concentration has been steadily declining HHL
 - the number of firms per worker as well as the labor share have risen
 - wage markdowns declining, despite price markups going up (Ding, Garcia-Louzao, and Jouvanceau, 2023)
 - flexicurity reforms in 2017

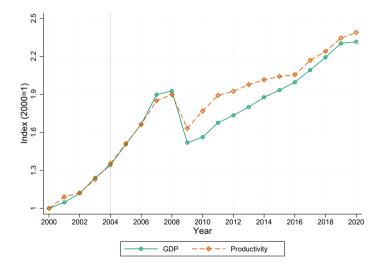
Contribution to the state of knowledge

- Firms explain around 20% of wage dispersion in developed economies and even more in developing countries (Card et al., 2013; Card et al. 2018; Alvarez et al., 2018; Song et al., 2019; Perez Perez and Nuno-Ledesma, 2022; Bassier, 2023)
 - + dynamics of firm-driven wage dispersion over the course of a country's development
- Measuring labor market power and its dynamics (Hirsch et al., 2018; Azar et al., 2022; Bassier et al., 2022; Lamadon et al., 2022; Diez et al., 2022; Webber, 2022; Armangue-Jubert et al., 2023)
 - + labor market competition in a context of economic growth
- Labor market power and wages (Webber 2015; Bassier, 2023; Autor et al., 2023; Deb et al., 2024)
 - + labor market competition as a driver of inequality
- Decreasing inequality in CEE typically linked to minimum wage legislation (Magda et al., 2021, Garcia-Louzao and Tarasonis, 2023)
 - + complementary explanation coming from market forces: competition

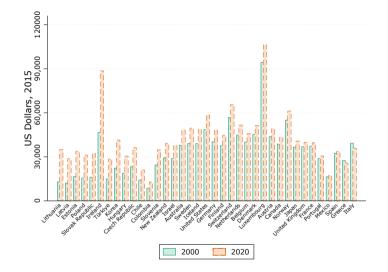
The fall of inequality under alternative indices



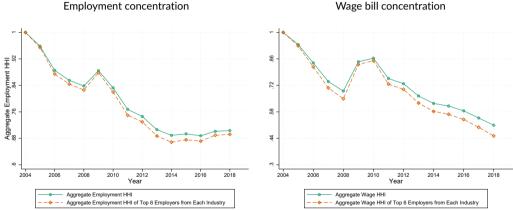
The Lithuanian economy experienced extraordinary economic growth



Among OECD countries, Lithuania experienced the largest growth in GDPpc

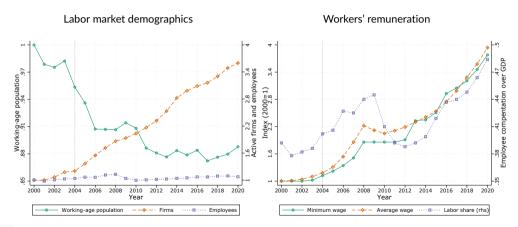


Labor market concentration computed from balance sheet data has been steadily decreasing



Wage bill concentration

EU accession unleashed in-house potential for new firms and created opportunities abroad for workers: LS \downarrow & LD \uparrow



Identification of worker and firm effects

- Connected set
 - only connected firms and their workers contribute to the identification
 - connected firms \equiv firms through which workers move
- Identifying assumptions
 - al exogenous mobility \rightarrow no correlation between mobility and the time-varying component of the residual
 - a2 additive separability \rightarrow no interaction of worker and firm heterogeneity
- Limited mobility bias
 - sufficient mobility to quantify the dispersion of firm-specific wage components
 - s1 KSS leave-one-out estimator to correct the bias (Kline et al., 2020)
 - s2 BLM firm-clusters to reduce dimensionality (Bonhomme et al., 2019, 2022)
- back

Summary statistics: Cleaned sample and connected set

| | 2000-2020 | | 2000 |)-2005 | 2015-2020 | | |
|-----------------|--------------|---------------|--------------|---------------|--------------|---------------|--|
| | Cleaned data | Connected set | Cleaned data | Connected set | Cleaned data | Connected set | |
| Wages | | | | | | | |
| Mean | 2.905 | 2.909 | 2.525 | 2.539 | 3.252 | 3.278 | |
| Std.Dev. | 0.779 | 0.777 | 0.764 | 0.759 | 0.679 | 0.667 | |
| Firms | 143,461 | 137,783 | 64,509 | 56,698 | 78,103 | 62,387 | |
| Direct movers | 296,159 | 295,942 | 124,873 | 124,425 | 124,595 | 123,530 | |
| Movers | 391,670 | 391,229 | 173,540 | 172,827 | 165,418 | 163,837 | |
| Workers | 532,495 | 526,536 | 330,161 | 320,625 | 333,238 | 314,337 | |
| Direct moves | 815,911 | 815,539 | 218,456 | 217,821 | 233,805 | 232,016 | |
| Job changes | 1,399,550 | 1,398,910 | 341,133 | 340,191 | 349,526 | 347,079 | |
| Worker-guarters | 16,735,572 | 16,638,459 | 4,510,485 | 4,409,926 | 4,957,606 | 4,696,179 | |

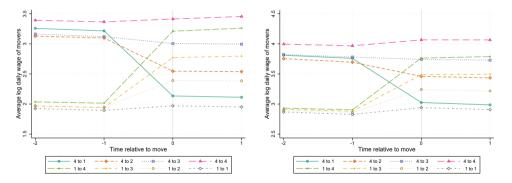
Firm and worker heterogeneity explain two-thirds of cross-sectional inequality

| | AKM | | KSS | KSS | | BLM | |
|-------------------------------|-----------|--------|-----------|--------|-----------|--------|--|
| | Component | Share | Component | Share | Component | Share | |
| Var(y) | 0.604 | - | 0.595 | - | 0.606 | - | |
| $Var(\eta)$ | 0.165 | 0.274 | 0.156 | 0.263 | 0.203 | 0.335 | |
| $Var(\psi)$ | 0.189 | 0.312 | 0.171 | 0.287 | 0.092 | 0.153 | |
| $Var(X\Omega)$ | 0.089 | 0.147 | 0.089 | 0.149 | 0.066 | 0.110 | |
| $Var(\epsilon)$ | 0.121 | 0.200 | 0.121 | 0.204 | 0.148 | 0.245 | |
| $2 \times Cov(\eta, \psi)$ | 0.041 | 0.068 | 0.053 | 0.088 | 0.078 | 0.129 | |
| $2 \times Cov(\eta, X\Omega)$ | -0.002 | -0.004 | -0.003 | -0.005 | -0.007 | -0.012 | |
| $2 \times Cov(\psi, X\Omega)$ | 0.002 | 0.003 | 0.003 | 0.004 | 0.024 | 0.040 | |

Wage changes after a switch by quarterly of firm fixed effects are near symmetric

(a) 2000-2005

(b) 2015-2020



Average residuals by deciles of worker and firm fixed effects suggest that match effects are not critical

| | - 9 | | +0.02 | -0.03 | -0.01 | 0.01 | 0.00 | 0.01 | 0.01 | 0.01 | 0.00 | 0.00 |
|---------------|-----|---|-------|-------|-------|--------|--------|--------|--------|-------|-------|-------|
| | o - | | -0.01 | -0.03 | -0.02 | -0.01 | 0.01 | 0.01 | 0.01 | 0.01 | 0.00 | 0.00 |
| e | ∞ - | | 0.00 | -0.01 | -0.02 | -0.01 | 0.01 | 0.01 | 0.01 | 0.00 | 0.00 | 0.00 |
| effect decile | | | 0.01 | -0.00 | -0.01 | -0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| | 9 - | | 0.00 | 0.01 | -0.01 | -0.01 | -0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| Worker fixed | - n | | 0.00 | 0.01 | 0.00 | -0.01 | -0.01 | -0.00 | -0.00 | 0.00 | -0.00 | 0.00 |
| orker | 4 - | | +0.00 | 0.02 | 0.01 | -0.00 | -0.01 | -0.01 | -0.01 | -0.00 | 0.00 | -0.00 |
| Š | ო - | | +0.00 | 0.01 | 0.02 | 0.00 | -0.00 | -0.01 | -0.01 | -0.01 | -0.00 | -0.01 |
| | ~ - | | 0.01 | -0.00 | 0.02 | 0.01 | -0.00 | -0.01 | -0.01 | -0.01 | -0.01 | -0.01 |
| | | | 0.03 | -0.00 | 0.00 | 0.01 | 0.00 | -0.00 | +0.00 | -0.01 | -0.02 | -0.01 |
| | | Ľ | | | | | | | | | | |
| | | | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| | | | | | F | Firm f | ixed e | effect | decile | Э | | |

(a) 2000-2005

(b) 2015-2020

| | 1 | | | | | | | | | | | |
|---------------|----------------|-------|-------|-------|--------|--------|-------|--------|-------|-------|-------|--|
| | - 9 | -0.00 | -0.00 | 0.00 | 0.01 | 0.01 | 0.00 | 0.00 | 0.00 | -0.00 | -0.00 | |
| | о - | -0.00 | -0.01 | 0.00 | 0.00 | 0.01 | 0.00 | 0.00 | 0.00 | -0.00 | -0.00 | |
| 0 | ∞ - | 0.00 | -0.01 | -0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | -0.00 | 0.00 | |
| effect decile | | 0.00 | -0.00 | -0.00 | -0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | |
| effed | 9 - | 0.00 | -0.01 | -0.00 | -0.00 | -0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | |
| Worker fixed | - <u>۲</u> | 0.01 | -0.00 | -0.00 | -0.01 | -0.00 | 0.00 | +0.00 | 0.00 | 0.00 | 0.01 | |
| orker | 4 - | 0.01 | 0.00 | -0.00 | -0.00 | -0.00 | +0.00 | -0.00 | 0.00 | 0.00 | 0.00 | |
| Ň | e - | 0.01 | 0.01 | 0.00 | -0.00 | -0.00 | +0.00 | +0.00 | -0.00 | -0.00 | -0.00 | |
| | - 5 | -0.01 | 0.01 | 0.00 | 0.00 | -0.00 | -0.01 | -0.00 | -0.00 | 0.00 | 0.00 | |
| | | -0.01 | 0.00 | 0.00 | 0.00 | 0.00 | -0.00 | -0.00 | -0.00 | 0.00 | -0.00 | |
| | l | | _ | _ | | 1 | _ | _ | _ | _ | - | |
| | | 1 | 2 | 3 | −irm f | 5 | | 7 | 8 | 9 | 10 | |
| | | | | | -irm i | ixed e | enect | decile | 9 | | | |

Contribution of workers and firms under alternative specifications of time-varying effects

| | Sex-specific ti | me effects | Wages cer | ntered | Residual w | ages |
|-------------------------------|-----------------|------------|-----------|--------|------------|-------|
| | Component | Share | Component | Share | Component | Share |
| Var(y) | 0.604 | - | 0.518 | - | 0.511 | - |
| $Var(\eta)$ | 0.170 | 0.281 | 0.164 | 0.317 | 0.163 | 0.319 |
| $Var(\psi)$ | 0.189 | 0.313 | 0.190 | 0.367 | 0.188 | 0.368 |
| $Var(X\Omega)$ | 0.090 | 0.149 | 0.007 | 0.013 | - | - |
| $Var(\epsilon)$ | 0.120 | 0.199 | 0.121 | 0.234 | 0.121 | 0.238 |
| $2 \times Cov(\eta, \psi)$ | 0.042 | 0.069 | 0.041 | 0.080 | 0.039 | 0.077 |
| $2 \times Cov(\eta, X\Omega)$ | -0.007 | -0.011 | -0.004 | -0.007 | - | - |
| $2 \times Cov(\psi, X\Omega)$ | 0.001 | 0.001 | -0.001 | -0.002 | - | - |

Contribution of workers and firms under alternative sample selection

| | LM attach | ment | MW | | Public se | ctor | No welfare b | enefits |
|-------------------------------------|-----------------|--------|-----------|--------|-----------|--------|--------------|---------|
| | Component Share | | Component | Share | Component | Share | Component | Share |
| Var(y) | 0.618 | - | 0.395 | - | 0.564 | - | 0.608 | - |
| $Var(\eta)$ | 0.178 | 0.289 | 0.146 | 0.369 | 0.183 | 0.325 | 0.169 | 0.300 |
| $Var(\psi)$ | 0.205 | 0.332 | 0.102 | 0.259 | 0.148 | 0.263 | 0.205 | 0.364 |
| $Var(X\Omega)$ | 0.088 | 0.143 | 0.077 | 0.194 | 0.088 | 0.156 | 0.100 | 0.177 |
| $Var(\epsilon)$ | 0.117 | 0.189 | 0.067 | 0.171 | 0.115 | 0.203 | 0.099 | 0.175 |
| $2 \times Cov(\eta, \psi)$ | 0.031 | 0.050 | 0.018 | 0.045 | 0.034 | 0.060 | 0.041 | 0.072 |
| $2 \times Cov(\eta, X\Omega)$ | -0.003 | -0.004 | -0.005 | -0.014 | -0.007 | -0.012 | -0.004 | -0.007 |
| $2 \times Cov(\psi, X\Omega)$ 0.000 | | 0.001 | -0.009 | -0.023 | 0.002 | 0.004 | -0.002 | -0.003 |

Contribution of workers and firms under alternative wage definitions to classify firms

| | BLM w/ worke | er variables | BLM w/ firm | variables |
|-------------------------------|--------------|--------------|-------------|-----------|
| | Component | Share | Component | Share |
| Var(y) | 0.607 | - | 0.607 | - |
| $Var(\eta)$ | 0.195 | 0.322 | 0.251 | 0.415 |
| $Var(\psi)$ | 0.103 | 0.170 | 0.074 | 0.122 |
| $Var(X\Omega)$ | 0.082 | 0.136 | 0.083 | 0.137 |
| $Var(\epsilon)$ | 0.145 | 0.238 | 0.153 | 0.252 |
| $2 \times Cov(\eta, \psi)$ | 0.078 | 0.128 | 0.044 | 0.072 |
| $2 \times Cov(\eta, X\Omega)$ | -0.004 | -0.007 | -0.007 | -0.011 |
| $2 \times Cov(\psi, X\Omega)$ | 0.008 | 0.013 | 0.009 | 0.015 |

Contribution of workers and firms under alternative number of firm clusters

| | BLM 15 | 50 | BLM 50 | 00 | BLM 25 | 00 |
|---------------------------------------|---|--------|-----------|--------|-----------|--------|
| | Component | Share | Component | Share | Component | Share |
| Var(y) | 0.606 | - | 0.606 | - | 0.606 | - |
| $Var(\eta)$ | 0.212 | 0.349 | 0.204 | 0.337 | 0.204 | 0.336 |
| $Var(\psi)$ | 0.088 | 0.145 | 0.091 | 0.151 | 0.094 | 0.154 |
| $Var(X\Omega)$ | 0.068 | 0.112 | 0.067 | 0.110 | 0.067 | 0.111 |
| $Var(\epsilon)$ | 0.150 | 0.247 | 0.149 | 0.245 | 0.148 | 0.244 |
| $2 \times Cov(\eta, \psi)$ | 0.074 | 0.121 | 0.078 | 0.129 | 0.077 | 0.127 |
| $2 \times Cov(\eta, X\Omega)$ | -0.007 | -0.012 | -0.007 | -0.012 | -0.007 | -0.012 |
| $2 	imes \textit{Cov}(\psi, X\Omega)$ | $\times Cov(\psi, X\Omega)$ 0.023 0.038 | | 0.024 | 0.040 | 0.024 | 0.040 |

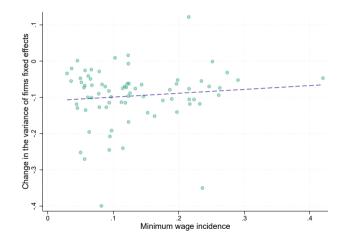
Contribution of workers and firms under alternative leave-one-out units

| | Leave-out-ob | servations | Leave-out-w | vorkers | |
|-------------------------------|--------------|------------|-------------|---------|--|
| | Component | Share | Component | Share | |
| Var(y) | 0.599 | - | 0.595 | - | |
| $Var(\eta)$ | 0.157 | 0.263 | 0.156 | 0.263 | |
| $Var(\psi)$ | 0.177 | 0.295 | 0.171 | 0.287 | |
| $Var(X\Omega)$ | 0.088 | 0.148 | 0.089 | 0.149 | |
| $Var(\epsilon)$ | 0.121 | 0.202 | 0.121 | 0.204 | |
| $2 \times Cov(\eta, \psi)$ | 0.050 | 0.084 | 0.053 | 0.089 | |
| $2 \times Cov(\eta, X\Omega)$ | -0.003 | -0.004 | -0.003 | -0.005 | |
| $2 \times Cov(\psi, X\Omega)$ | 0.002 | 0.004 | 0.003 | 0.004 | |

Sectoral decomposition

| | | AKM | | BLM |
|-----------------------|-----------------|-------------------------|-----------------|-------------------------|
| | Estimate (1) | Contribution (%) (2) | Estimate (3) | Contribution (%) (4) |
| Change in $Var(y)$ | -0.131 | - | -0.136 | - |
| Change in $Var(\psi)$ | -0.118 | 89.8 | -0.127 | 93.0 |
| Between-sector | 0.016 | -12.1 | 0.006 | -4.5 |
| Within-sector | -0.134 | 112.1 | -0.133 | 104.5 |

Variance of firm fixed effects vs MW



Separation elasticity using a complementary log-log model

| A. 2000-2005 | Worke | er wage | IV-Firm fi | xed effect |
|--------------|-----------|-----------|------------|------------|
| | Sep | EE Sep | Sep | EE Sep |
| Esep | -0.5550 | -0.4747 | -0.6712 | -0.7611 |
| , | (0.0034) | (0.0046) | (0.0366) | (0.0481) |
| | | | | |
| Observations | 4,149,923 | 4,149,923 | 4,149,923 | 4,149,923 |
| | | | | |
| B. 2015-2020 | Worke | er wage | IV-Firm fi | xed effect |
| | Sep | EE Sep | Sep | EE Sep |
| Esep | -0.6692 | -0.5086 | -0.8459 | -0.8666 |
| | (0.0037) | (0.0050) | (0.0203) | (0.0224) |
| | | | | |
| Observations | 4,404,064 | 4,404,064 | 4,404,064 | 4,404,064 |

Separation elasticity using alternative controls

| A. 2000-2005 | | | | Worke | r wage | | | | | | | IV-Firm fi | xed effect | | | |
|------------------------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|------------|------------|-----------|-----------|-----------|
| | Sep | EE Sep | Sep | EE Sep | Sep | EE Sep |
| Esep | -0.0475 | -0.0209 | -0.0622 | -0.0269 | -0.0598 | -0.0249 | -0.0647 | -0.0191 | -0.0627 | -0.0379 | -0.0815 | -0.0472 | -0.0794 | -0.0431 | -0.0989 | -0.0460 |
| | (0.0004) | (0.0003) | (0.0004) | (0.0003) | (0.0004) | (0.0003) | (0.0003) | (0.0002) | (0.0022) | (0.0014) | (0.0023) | (0.0015) | (0.0024) | (0.0014) | (0.0024) | (0.0014) |
| Observations | 4,149,923 | 4,149,923 | 4,149,923 | 4,149,923 | 4,149,923 | 4,149,923 | 4,149,923 | 4,149,923 | 4,149,923 | 4,149,923 | 4,149,876 | 4,149,876 | 4,149,923 | 4,149,923 | 4,149,923 | 4,149,923 |
| A. 2015-2020 | | | | Worke | r wage | | | | | | | IV-Firm fi | xed effect | | | |
| | Sep | EE Sep | Sep | EE Sep | Sep | EE Sep |
| Esep | -0.0684 | -0.0254 | -0.0795 | -0.0298 | -0.0766 | -0.0288 | -0.0750 | -0.0222 | -0.0851 | -0.0457 | -0.1062 | -0.0666 | -0.0969 | -0.0503 | -0.1394 | -0.0601 |
| | (0.0004) | (0.0003) | (0.0005) | (0.0003) | (0.0005) | (0.0003) | (0.0004) | (0.0002) | (0.0021) | (0.0013) | (0.0025) | (0.0015) | (0.0023) | (0.0013) | (0.0026) | (0.0015) |
| Observations | 4,404,064 | 4,404,064 | 4,404,064 | 4,404,064 | 4,404,064 | 4,404,064 | 4,404,064 | 4,404,064 | 4,404,064 | 4,404,064 | 4,404,024 | 4,404,024 | 4,404,064 | 4,404,064 | 4,404,064 | 4,404,064 |
| Tenure FE | Y | Y | N | N | N | N | N | N | Y | Y | N | N | N | N | N | N |
| Sector×Municipality FE | N | N | Y | Y | N | N | N | N | N | N | Y | Y | N | N | N | N |
| Family controls | N | N | N | N | Y | Y | N | N | N | N | N | N | Y | Y | N | N |
| AKM worker type | Y | Y | Y | Y | Y | Y | N | N | Y | Y | Y | Y | Y | Y | N | N |

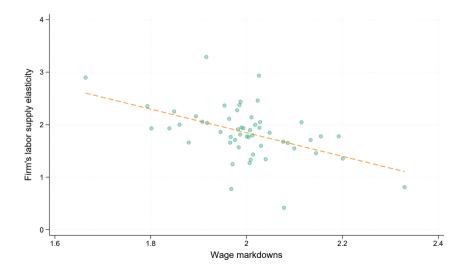
Elasticity for workers with FE below median

| A. 2000-2005 | Worke | r wage | Firm fixe | ed effect | IV-Firm fi | IV-Firm fixed effect | | |
|-------------------------|-----------|-----------|-----------|-----------|------------|----------------------|--|--|
| | Sep | EE Sep | Sep | EE Sep | Sep | EE Sep | | |
| | (1) | (2) | (3) | (4) | (5) | (6) | | |
| β | -0.0674 | -0.0235 | -0.0552 | -0.0241 | -0.0856 | -0.0451 | | |
| | (0.0007) | (0.0004) | (0.0029) | (0.0013) | (0.0036) | (0.0018) | | |
| ϵ_{LS} | 0.9520 | 0.8651 | 0.7798 | 0.8872 | 1.2093 | 1.6626 | | |
| | (0.0092) | (0.0148) | (0.0413) | (0.0462) | (0.0514) | (0.0665) | | |
| First stage F-statistic | | | | | 2,32 | 8.86 | | |
| Observations | 2,074,976 | 2,074,976 | 2,074,976 | 2,074,976 | 2,074,976 | 2,074,976 | | |
| | | | | | | | | |
| B. 2015-2020 | Worke | r wage | Firm fixe | ed effect | IV-Firm fi | xed effect | | |
| | Sep | EE Sep | Sep | EE Sep | Sep | EE Sep | | |
| | (1) | (2) | (3) | (4) | (5) | (6) | | |
| β | -0.0875 | -0.0271 | -0.0730 | -0.0299 | -0.1036 | -0.0538 | | |
| | (0.0007) | (0.0005) | (0.0021) | (0.0011) | (0.0036) | (0.0019) | | |
| ϵ_{LS} | 1.3317 | 1.0121 | 1.1122 | 1.1173 | 1.5776 | 2.0090 | | |
| 20 | (0.0112) | (0.0178) | (0.0317) | (0.0428) | (0.0550) | (0.0695) | | |
| First stage F-statistic | | | | | 9,97 | 5.29 | | |
| Observations | 2,202,037 | 2,202,037 | 2,202,037 | 2,202,037 | 2.202.037 | 2,202,037 | | |

Elasticity for workers with FE above median

| A. 2000-2005 | Worke | r wage | Firm fixe | ed effect | IV-Firm fi | IV-Firm fixed effect | | |
|-------------------------|-----------|-----------|-----------|-----------|------------|----------------------|--|--|
| | Sep | EE Sep | Sep | EE Sep | Sep | EE Sep | | |
| | (1) | (2) | (3) | (4) | (5) | (6) | | |
| β | -0.0526 | -0.0249 | -0.0403 | -0.0185 | -0.0742 | -0.0405 | | |
| | (0.0005) | (0.0004) | (0.0015) | (0.0010) | (0.0020) | (0.0014) | | |
| ϵ_{LS} | 1.1529 | 1.0236 | 0.8842 | 0.7613 | 1.6261 | 1.6690 | | |
| | (0.0108) | (0.0148) | (0.0332) | (0.0425) | (0.0430) | (0.0570) | | |
| First stage F-statistic | | | | | 3,57 | 6.39 | | |
| Observations | 2,074,947 | 2,074,947 | 2,074,947 | 2,074,947 | 2,074,947 | 2,074,947 | | |
| | | | | | | | | |
| B. 2015-2020 | Worke | r wage | Firm fixe | ed effect | IV-Firm fi | xed effect | | |
| | Sep | EE Sep | Sep | EE Sep | Sep | EE Sep | | |
| | (1) | (2) | (3) | (4) | (5) | (6) | | |
| β | -0.0668 | -0.0293 | -0.0417 | -0.0193 | -0.0910 | -0.0474 | | |
| , | (0.0006) | (0.0004) | (0.0014) | (0.0010) | (0.0021) | (0.0014) | | |
| ϵ_{LS} | 1.4158 | 1.1625 | 0.8840 | 0.7665 | 1.9285 | 1.8814 | | |
| - 10 | (0.0134) | (0.0175) | (0.0301) | (0.0394) | (0.0449) | (0.0562) | | |
| First stage F-statistic | | | | | 10,122.45 | | | |
| Observations | 2,202,027 | 2,202,027 | 2,202,027 | 2,202,027 | 2,202,027 | 2,202,027 | | |

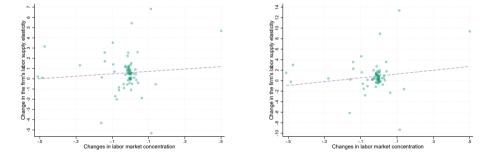
Firms' labor supply elasticity and wage markdowns across datasets



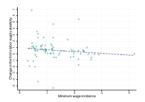
Firm granularity: Elasticity vs concentration

(a) All separations





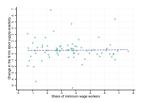
Firm granularity: Elasticity vs MW

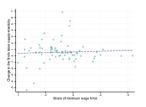


(a) MW incidence

(b) MW workers







Contribution of changes in competition to changes in overall wage inequality

The contribution of competition to overall inequality can be calculated as

$$\sum_{s=1}^{S} \frac{L_{st}}{L_t} \hat{\beta}_1 \Delta \varepsilon_{st+1}$$

- *L* is the number of workers
- $\hat{\beta}_1$ is the effect of competition on the variance of firm fixed effects
- ε_s sector-specific firm labor supply elasticity

Changes in labor market competition can explain a reduction in wage inequality through firm-specific wage components equal to

$$0.9 \times \left(\frac{\sum_{s=1}^{S} \frac{L_{st}}{L_t} \hat{\beta}_1 \Delta \varepsilon_{st+1}}{\sum_{s=1}^{S} \frac{L_{st}}{L_t} \Delta \mathsf{var}_{st+1}[\psi_{jt+1}]}\right) \times 100\%$$



Increased competition in the labor market does not affect the dispersion of worker fixed effects or sorting

| A. $\Delta var_{st+1}[\eta]$ | Worker wage | | Iv-Firm fixed effect | |
|--|----------------------|---------------------|-----------------------|---------------------|
| | OLS | IV | OLS | IV |
| | (1) | (2) | (3) | (4) |
| Δ Firm LSE | -0.0248 | 0.0848 | -0.0174 | -0.0218 |
| | (0.0352) | (0.1108) | (0.0090) | (0.0189) |
| | Worker wage | | IV-Firm fixed effect | |
| B. $\Delta \text{cov}_{st+1}[\psi, \eta]$ | Worke | r wage | IV-Firm fi | xed effect |
| B. $\Delta \text{cov}_{st+1}[\psi, \eta]$ | Worke OLS | r wage IV | IV-Firm fi | xed effect IV |
| B. $\Delta \text{cov}_{st+1}[\psi, \eta]$ | | | | |
| B. $\Delta \text{cov}_{st+1}[\psi, \eta]$ Δ Firm LSE | OLS | ĪV | OLS | IV |
| | OLS (1) | IV (2) | OLS (3) | IV (4) |
| | OLS (1) 0.0121 | IV (2) 0.0098 | OLS (3) -0.0090 | IV (4) 0.0293 |